



	Year 3			
Year 3 Addition	Concrete	Pictorial	Abstract	
Understanding 100s	Understand the cardinality of 100, and the link with 10 tens. Use cubes to place into groups of 10 tens.	Unitise 100 and count in steps of 100.	Represent steps of 100 on a number line and a number track and count up to 1,000 and back to 0.	
Understanding place value to 1,000	Unitise 100s, 10s and 1s to build 3-digit numbers.	Use equipment to represent numbers to 1,000.	Represent the parts of numbers to 1,000 using a part-whole model. 215 = 200 + 10 + 5 Recognise numbers to 1,000 represented on a number line, including those between intervals.	





Adding 100s	Use known facts and unitising to add multiples of 100.	Use known facts and unitising to add multiples of 100.	Use known facts and unitising to add multiples of 100.
	100 bricks + 100 bricks $100 loo + 100 bricks$ $100 bricks + 200 bricks$ $3 + 2 = 5$ $3 hundreds + 2 hundreds = 5 hundreds$ $300 + 200 = 500$	3 + 4 = 7 3 hundreds + 4 hundreds = 7 hundreds 300 + 400 = 700	Represent the addition on a number line. Use a part-whole model to support unitising. 3 + 2 = 5 300 + 200 = 500
3-digit number	Use number bonds to add the 1s.	Use number bonds to add the 1s.	Understand the link with counting on.
+ 1s, no exchange or bridging	214 + 4 = ? Now there are 4 + 4 ones in total.	HTOImage: Second stateImage: Secon	245 + 4 245 + 4 245 246 247 248 249 250 Use number bonds to add the 1s and understand that this is more efficient and less prone to error.
	4 + 4 = 8 214 + 4 = 218	5 + 4 = 9 245 + 4 = 249	245 + 4 = ?
			5 + 4 = 9 So, 245 + 4 = 249





3-digit number + 1s with exchange	Understand that when the 1s sum to 10 or more, this requires an exchange of 10 ones for 1 ten.	Exchange 10 ones for 1 ten where needed. Use a place value grid to support the understanding.	
	objects or physical apparatus.		
		H T O	
		H T O	
		135 + 7 = 142	





3-digit number + 10s, no	Calculate mentally by forming the number bond for the 10s.	Calculate mentally by forming the number bond for the 10s.	Calculate mentally by forming the number bond for the 10s.
exchange	234 + 50 There are 3 tens and 5 tens altogether. 3 + 5 = 8 In total there are 8 tens. 234 + 50 = 284	351 + 30 = ? $4 + 7 + 0$ $4 + 7 + 0$ $4 + 7 + 0$ $4 + 7 + 0$ $4 + 7 + 0$ $4 + 7 + 0$ $4 + 7 + 0$ $5 tens + 3 tens = 8 tens$ $351 + 30 = 381$	753 + 40 I know that 5 + 4 = 9 So, 50 + 40 = 90 753 + 40 = 793
3-digit number + 10s, with exchange	Understand the exchange of 10 tens for 1 hundred.	Add by exchanging 10 tens for 1 hundred. 184 + 20 = ? H T O B T O	Understand how the addition relates to counting on in 10s across 100. 100 184 + 20 = ? <i>I can count in 10s 194 204</i> 184 + 20 = 204 Use number bonds within 20 to support efficient mental calculations. 385 + 50 There are 8 tens and 5 tens. That is 13 tens. 385 + 50 = 300 + 130 + 5 385 + 50 = 435





3-digit number + 2-digit number	Use place value equipment to make and combine groups to model addition.	Use a place value grid to organise thinking and adding of 1s, then 10s.	Use the vertical column method to represent the addition. Children must understand how this relates to place value at each stage of the calculation.
3-digit number + 2-digit number, exchange required	Use place value equipment to model addition and understand where exchange is required. Use place value counters to represent 154 + 72. Use this to decide if any exchange is required. There are 5 tens and 7 tens. That is 12 tens so I will exchange.	Represent the required exchange on a place value grid using equipment. $275 + 16 = ?$ $\frac{1}{100}$ \frac	Use a column method with exchange. Children must understand how the method relates to place value at each stage of the calculation. $\frac{H T O}{2 7 5} + \frac{1 6}{1 6}$ $\frac{H T O}{2 7 5} + \frac{1 6}{1 6}$ $\frac{H T O}{2 7 5} + \frac{1 6}{2 9 1}$ $275 + 16 = 291$





3-digit number + 3-digit number, no exchange	Use place value equipment to make a representation of a calculation. This may or may not be structured in a place value grid. 326 + 541 is represented as: H = T = 0 326 5 4 1	Represent the place value grid with equipment to model the stages of column addition.	Use a column method to solve efficiently, using known bonds. Children must understand how this relates to place value at every stage of the calculation.
3-digit number + 3-digit number, exchange required	Use place value equipment to enact the exchange required.	Model the stages of column addition using place value equipment on a place value grid.	Use column addition, ensuring understanding of place value at every stage of the calculation. $\frac{\frac{H}{1} T 0}{\frac{1}{2} 6}$ $\frac{\frac{H}{2} \frac{T}{1} \frac{7}{\frac{3}{4} \frac{3}{3}}}{\frac{1}{2}}$ $\frac{\frac{H}{1} T 0}{\frac{1}{2} 6}$ $\frac{\frac{H}{2} \frac{T}{1} \frac{7}{\frac{3}{4} \frac{3}{3}}}{\frac{1}{3}}$ $\frac{126 + 217 = 343}{1}$ Note: Children should also study examples where exchange is required in more than one column, for example $185 + 318 = ?$





Representing addition	Encourage children to use their own drawings and choices of place value	Children understand and create bar models to represent addition problems.	Use representations to support choices of appropriate methods.
selecting appropriate methods	or more steps. These representations will help them to select appropriate methods.	$275 + 99 = ?$ 374 $275 \qquad qq$? 275 1 will add 100, then subtract 1 to find the
		275 + 99 = 374	solution. 128 + 105 + 83 = ? I need to add three numbers. 128 + 105 = 233
			233 128 105 83 316
			233 83





Year 3 Subtraction	Concrete	Pictorial	Abstract
Subtracting 100s	Use known facts and unitising to subtract multiples of 100. 100 bricks 5 - 2 = 3 500 - 200 = 300	Use known facts and unitising to subtract multiples of 100. 4 - 2 = 2 400 - 200 = 200	Understand the link with counting back in 100s. 100 100 200 300 400 $500400 - 200 = 200Use known facts and unitising as efficientand accurate methods.I know that 7 - 4 = 3. Therefore, I know that700 - 400 = 300$.
3-digit number − 1s, no exchange	Use number bonds to subtract the 1s. Use number bonds to subtract the 1s. 214 - 3 = ? 14 - 3 = ? 4 - 3 = 1 214 - 3 = 211	Use number bonds to subtract the 1s. $ \begin{array}{c c} H & T & O \\ \hline & & & & \\ & & & & \\ \hline & & & & \\ & & & & \\ & & & & \\ & & & &$	Understand the link with counting back using a number line. Use known number bonds to calculate mentally. 476 - 4 = ? 476 - 4 = ? 476 - 4 = ? 6 - 4 = 2 476 - 4 = 472





3-digit number − 1s, exchange or bridging required	Understand why an exchange is necessary by exploring why 1 ten must be exchanged. Use place value equipment.	Represent the required exchange on a place value grid. 151 - 6 = ? H T O H T O H T O H T O N N N N N N N N N N N N N N N N N N N	Calculate mentally by using known bonds. 151 - 6 = ? 151 - 1 - 5 = 145
3-digit number − 10s, no exchange	Subtract the 10s using known bonds. 381 - 10 = ? 8 tens with 1 removed is 7 tens. 381 - 10 = 371	Subtract the 10s using known bonds. $\begin{array}{c c} H & T & O \\ \hline $	Use known bonds to subtract the 10s mentally. 372 - 50 = ? 70 - 50 = 20 So, 372 - 50 = 322





3-digit number − 10s, exchange or bridging required	Use equipment to understand the exchange of 1 hundred for 10 tens.	Represent the exchange on a place value grid using equipment. 210 - 20 = ? H T O I need to exchange 1 hundred for 10 tens, to help subtract 2 tens. H T O I 0 I	
3-digit number − up to 3-digit number	Use place value equipment to explore the effect of splitting a whole into two parts, and understand the link with taking away.	Represent the calculation on a place value grid.	Use column subtraction to calculate accurately and efficiently. $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$





3-digit number – up to 3-digit number	Use equipment to enact the exchange of 1 hundred for 10 tens, and 1 ten for 10 ones.	Model the required exchange on a place value grid.	Use column subtraction to work accurately and efficiently.
number, exchange required	$ \rightarrow \qquad \vdots \qquad$	175 - 38 = ? I need to subtract 8 ones, so I will exchange a ten for 10 ones. $H T O$ $H T O$ $H T O$ $H T O$	$\frac{H T O}{I \frac{6}{4} \frac{15}{5}}$ $-\frac{3 8}{I \frac{3 7}{2}}$ $\frac{175 - 38 = 137}{I75 - 38 = 137}$ If the subtraction is a 3-digit number subtract a 2-digit number, children should understand how the recording relates to the place value, and so how to line up the digits correctly. Children should also understand how to exchange in calculations where there is a
		H T O	zero in the 10s column.
Representing subtraction problems		Use bar models to represent subtractions. 'Find the difference' is represented as two bars for comparison. Team A 454 Team B 128 ? Bar models can also be used to show that a part must be taken away from the whole.	Children use alternative representations to check calculations and choose efficient methods. Children use inverse operations to check additions and subtractions. The part-whole model supports understanding. <i>I have completed this subtraction.</i> 525 - 270 = 255 <i>I will check using addition.</i>





Year 3 Multiplication	Concrete	Pictorial	Abstract
Understanding equal grouping and repeated addition	Children continue to build understanding of equal groups and the relationship with repeated addition. They recognise both examples and non- examples using objects.	Children recognise that arrays demonstrate commutativity. This is 3 groups of 4. This is 4 groups of 3.	Children understand the link between repeated addition and multiplication. $ \begin{array}{c} +3 & +3 & +3 & +3 & +3 & +3 & +3 & +3 \\ \hline 0 & 3 & 6 & q & 12 & 15 & 18 & 21 & 24 \\ \hline 0 & 3 & 6 & q & 12 & 15 & 18 & 21 & 24 \\ \hline 8 groups of 3 is 24. \\ 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 = 24 \\ 8 \times 3 = 24 \\ \hline A \text{ bar model may represent multiplications as equal groups.} \\ \hline \begin{array}{c} 24 \\ \hline 4 & 4 & 4 & 4 & 4 \\ \hline 6 \times 4 = 24 \\ \end{array} $





Using commutativity to support understanding of the times- tables	Understand how to use times-tables facts flexibly.	Understand how times-table facts relate to commutativity.	Understand how times-table facts relate to commutativity. I need to work out 4 groups of 7. I know that $7 \times 4 = 28$ so, I know that 4 groups of $7 = 28$ and 7 groups of $4 = 28$.
	There are 6 groups of 4 pens. There are 4 groups of 6 bread rolls. I can use $6 \times 4 = 24$ to work out both totals.		
Understanding and using ×3, ×2, ×4 and ×8 tables.	Children learn the times-tables as 'groups of', but apply their knowledge of commutativity. Image: Commutativity is the intervention of the i	Children understand how the x2, x4 and x8 tables are related through repeated doubling.	Children understand the relationship between related multiplication and division facts in known times-tables. $2 \times 5 = 10$ $5 \times 2 = 10$ $10 \div 5 = 2$ $10 \div 2 = 5$





Using known facts to multiply 10s, for example 3 × 40	Explore the relationship between known times-tables and multiples of 10 using place value equipment. <i>Make 4 groups of 3 ones.</i> <i>Make 4 groups of 3 tens.</i> <i>Make 4 groups of 3 tens.</i> <i>What is the same?</i> <i>What is different?</i>	Understand how unitising 10s supports multiplying by multiples of 10. 1 1 1 1 1 11 1 1 1 11 1 1 1 1 11 1 1 1 1 11 1 1 1 1 1 11 1 1 1 1 1 1 1 1 11 1 1 1 1 1 1 1 1 1	Understand how to use known times-tables to multiply multiples of 10. $\begin{array}{r} +2 +2 +2 +2 +2 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \end{array}$ $\begin{array}{r} +20 +20 +20 +20 \\ \hline 0 & 10 & 20 & 30 & 40 & 50 & 60 & 70 & 80 \end{array}$ $\begin{array}{r} +20 +20 +20 +20 \\ \hline 0 & 10 & 20 & 30 & 40 & 50 & 60 & 70 & 80 \end{array}$ $\begin{array}{r} 4 \times 2 = 8 \\ 4 \times 20 = 80 \end{array}$
Multiplying a 2-digit number by a 1-digit number	Understand how to link partitioning a 2-digit number with multiplying. Each person has 23 flowers. Each person has 2 tens and 3 ones. Each person has 2 tens and 3 ones. There are 3 groups of 2 tens. There are 3 groups of 3 ones.	$4 \times 2 = 8$ $4 \times 20 = 80$ Use place value to support how partitioning is linked with multiplying by a 2-digit number. $3 \times 24 = ?$ $T \qquad 0$ $3 \times 4 = 12$	Use addition to complete multiplications of 2-digit numbers by a 1-digit number. $4 \times 13 = ?$ $4 \times 3 = 12$ $4 \times 10 = 40$ 12 + 40 = 52 $4 \times 13 = 52$











	4 × 23 = 92	<u>T O</u> 2 8
	$5 \times 23 = ?$ $5 \times 3 = 15$ $5 \times 20 = 100$ $5 \times 23 = 115$	





Year 3 Division	Concrete	Pictorial	Abstract
Using times- tables knowledge to divide	Use knowledge of known times-tables to calculate divisions. 24 divided into groups of 8. There are 3 groups of 8.	Use knowledge of known times-tables to calculate divisions. Use knowledge of known times-tables to calculate divisions. Use knowledge of known times-tables to calculate divisions. $48 \div 4 = 12$ 48 divided into groups of 4. There are 12 groups. $4 \times 12 = 48$ $48 \div 4 = 12$	Use knowledge of known times-tables to calculate divisions. I need to work out 30 shared between 5. I know that $6 \times 5 = 30$ so I know that $30 \div 5 = 6$. A bar model may represent the relationship between sharing and grouping. 24 4 4 4 4 4 4 4 4 4





Understanding remainders Using known	Use equipment to understand that a remainder occurs when a set of objects cannot be divided equally any further.	Use images to explain remainders.	Understand that the remainder is what cannot be shared equally from a set. $22 \div 5 = ?$ $3 \times 5 = 15$ $4 \times 5 = 20$ $5 \times 5 = 25 \dots$ this is larger than 22 So, $22 \div 5 = 4$ remainder 2 Divide multiples of 10 by a single digit using
facts to divide multiples of 10	how to divide by unitising. Make 6 ones divided by 3. Now make 6 tens divided by 3. What is the same? What is different?	12 tens shared into 3 equal groups. 4 tens in each group.	Known times-tables. $180 \div 3 = ?$ 180 is 18 tens. 18 divided by 3 is 6. 18 tens divided by 3 is 6 tens. $18 \div 3 = 6$ $180 \div 3 = 60$
2-digit number divided by 1-digit number, no remainders	Children explore dividing 2-digit numbers by using place value equipment. $48 \div 2 = ?$ First divide the 10s.	Children explore which partitions support particular divisions.	Children partition a number into 10s and 1s to divide where appropriate. 68 $60 \div 2 = 30$ $8 \div 2 = 4$ $30 + 4 = 34$ $68 \div 2 = 34$ Children partition flexibly to divide where





	Then divide the 1s.	3. 42 30 12	appropriate. $42 \div 3 = ?$ 42 = 40 + 2 <i>I need to partition 42 differently to divide</i> <i>by 3.</i> 42 = 30 + 12 $30 \div 3 = 10$ $12 \div 3 = 4$ 10 + 4 = 14 $42 \div 3 = 14$
2-digit number divided by 1-digit number, with remainders	Use place value equipment to understand the concept of remainder. <i>Make 29 from place value equipment.</i> <i>Share it into 2 equal groups.</i> There are two groups of 14 and 1 remainder.	Use place value equipment to understand the concept of remainder in division. $29 \div 2 = ?$ $29 \div 2 = 14$ remainder 1	Partition to divide, understanding the remainder in context. 67 children try to make 5 equal lines. 67 = 50 + 17 $50 \div 5 = 10$ $17 \div 5 = 3$ remainder 2 $67 \div 5 = 13$ remainder 2 There are 13 children in each line and 2 children left out.