



#### LOWER KEY STAGE 2

In Years 3 and 4, children develop the basis of written methods by building their skills alongside a deep understanding of place value. They should use known addition/subtraction and multiplication/division facts to calculate efficiently and accurately, rather than relying on counting. Children use place value equipment to support their understanding, but not as a substitute for thinking.

Key language: partition, place value, tens, hundreds, thousands, column method, whole, part, equal groups, sharing, grouping, bar model

Addition and subtraction: In Year 3 especially, the column methods are built up gradually. Children will develop their understanding of how each stage of the calculation, including any exchanges, relates to place value. The example calculations chosen to introduce the stages of each method may often be more suited to a mental method. However, the examples and the progression of the steps have been chosen to help children develop their fluency in the process, alongside a deep understanding of the concepts and the numbers involved, so that they can apply these skills accurately and efficiently to later calculations. The class should be encouraged to compare mental and written methods for specific calculations, and children should be encouraged at every stage to make choices about which methods to apply. In Year 4, the steps are shown without such fine

In Year 4, the steps are shown without such fine detail, although children should continue to build their understanding with a secure basis in place value. In subtraction, children will need to develop their understanding of exchange as they may need to exchange across one or two columns. By the end of Year 4, children should have developed fluency in column methods alongside a deep understanding, which will allow them to progress confidently in upper Key Stage 2. Multiplication and division: Children build a solid grounding in times-tables, understanding the multiplication and division facts in tandem. As such, they should be as confident knowing that 35 divided by 7 is 5 as knowing that 5 times 7 is 35. Children develop key skills to support multiplication methods: unitising, commutativity, and how to use partitioning effectively. Unitising allows children to use known facts to multiply and divide multiples of 10 and 100 efficiently. Commutativity gives children flexibility in applying known facts to calculations and problem solving. An understanding of partitioning allows children to extend their skills to multiplying and dividing 2- and 3-digit numbers by a single digit.

Children develop column methods to support multiplications in these cases.

For successful division, children will need to make choices about how to partition. For example, to divide 423 by 3, it is effective to partition 423 into 300, 120 and 3, as these can be divided by 3 using known facts.

Children will also need to understand the concept of remainder, in terms of a given calculation and in terms of the context of the problem. **Fractions:** Children develop the key concept of equivalent fractions, and link this with multiplying and dividing the numerators and denominators, as well as exploring the visual concept through fractions of shapes. Children learn how to find a fraction of an amount and develop this with the aid of a bar model and other representations alongside.

in Year 3, children develop an understanding of how to add and subtract fractions with the same denominator and find complements to the whole. This is developed alongside an understanding of fractions as numbers, including fractions greater than 1. In Year 4, children begin to work with fractions greater than 1.

Decimals are introduced, as tenths in Year 3 and then as hundredths in Year 4. Children develop an understanding of decimals in terms of the relationship with fractions, with dividing by 10 and 100, and also with place value.





	Year 3			
	Concrete	Pictorial	Abstract	
Year 3 Addition				
Understanding 100s	Understand the cardinality of 100, and the link with 10 tens. Use cubes to place into groups of 10 tens.	Unitise 100 and count in steps of 100.	Represent steps of 100 on a number line and a number track and count up to 1,000 and back to 0.	
Understanding place value to 1,000	Unitise 100s, 10s and 1s to build 3-digit numbers.	Use equipment to represent numbers to 1,000. 200 240 241 241 241 Use a place value grid to support the structure of numbers to 1,000. Place value counters are used alongside other equipment. Children should understand how each counter represents a different unitised amount.	Represent the parts of numbers to 1,000 using a part-whole model. 215 200 $10$ $5215 = 200 + 10 + 5Recognise numbers to 1,000 representedon a number line, including those betweenintervals.$	





Adding 100s	Use known facts and unitising to add multiples of 100.	Use known facts and unitising to add multiples of 100.	Use known facts and unitising to add multiples of 100.
	100 bricks $100$ bricks $100$ bricks $100$ bricks $3 + 2 = 5$ $3  hundreds + 2  hundreds = 5  hundreds$ $300 + 200 = 500$	3 + 4 = 7 3 hundreds + 4 hundreds = 7 hundreds 300 + 400 = 700	Represent the addition on a number line. Use a part-whole model to support unitising. 3 + 2 = 5 $300 + 200 = 500$
3-digit number + 1s, no exchange or bridging	Use number bonds to add the 1s. Use number bonds to add the 1s. 1000000000000000000000000000000000000	Use number bonds to add the 1s. $ \begin{array}{c c} \hline H & T & O \\ \hline \hline 0 & 0 & 0 & 0 \\ \hline \hline 2 & 4 & 9 \\ \hline 245 + 4 \\ 5 + 4 = 9 \\ \hline 245 + 4 = 249 \\ \end{array} $	Understand the link with counting on. 245 + 4 4 4 4 4 4 4 4





			So, 245 + 4 = 249
3-digit number + 10s, no exchange	Calculate mentally by forming the number bond for the 10s.	Calculate mentally by forming the number bond for the 10s.	Calculate mentally by forming the number bond for the 10s.
exchange	234 + 50 There are 3 tens and 5 tens altogether. $3 + 5 = 8$ In total there are 8 tens. $234 + 50 = 284$	351 + 30 = ? $H T O$ $H T O$ $I O$	753 + 40 I know that 5 + 4 = 9 So, 50 + 40 = 90 753 + 40 = 793
3-digit number + 1s with exchange	Understand that when the 1s sum to 10 or more, this requires an exchange of 10 ones for 1 ten. Children should explore this using unitised objects or physical apparatus.	Exchange 10 ones for 1 ten where needed. Use a place value grid to support the understanding.	Understand how to bridge by partitioning to the 1s to make the next 10. 7 5 2 135 140 142
		H T O 135 + 7 = 142	135 + 7 = ? 135 + 5 + 2 = 142 Ensure that children understand how to ad 1s bridging a 100.

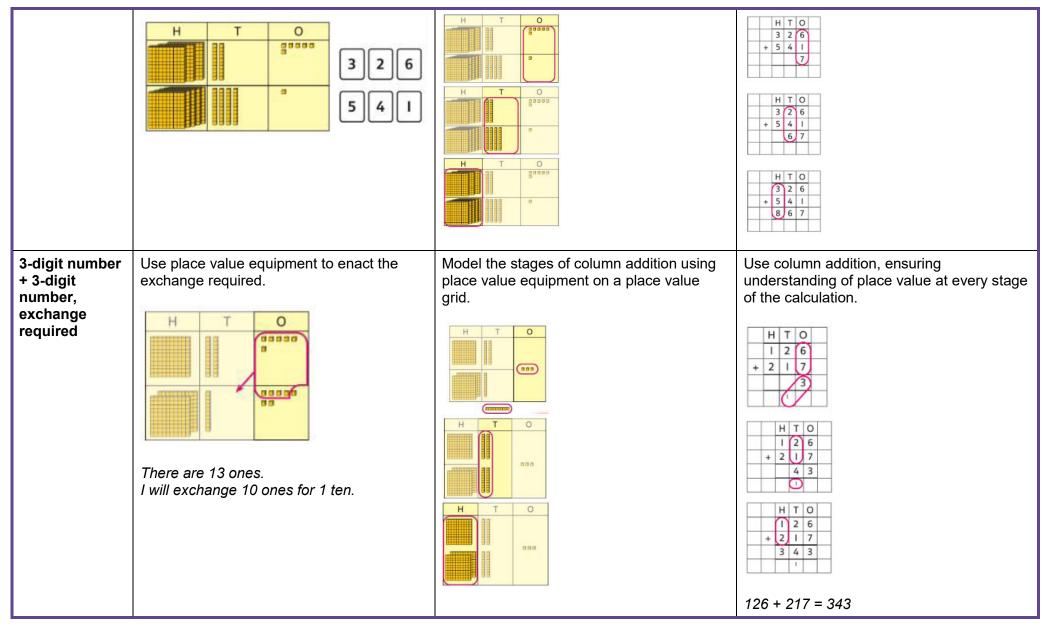




3-digit number + 10s, with exchange	Understand the exchange of 10 tens for 1 hundred.	Add by exchanging 10 tens for 1 hundred. 184 + 20 = ? H T O H T O	198 + 5 = ? $198 + 2 + 3 = 203$ Understand how the addition relates to counting on in 10s across 100. $100 + 10$
3-digit number + 3-digit number, no exchange	Use place value equipment to make a representation of a calculation. This may or may not be structured in a place value grid. 326 + 541 is represented as:	Represent the place value grid with equipment to model the stages of column addition.	Use a column method to solve efficiently, using known bonds. Children must understand how this relates to place value at every stage of the calculation.











			<i>Note:</i> Children should also study examples where exchange is required in more than one column, for example <i>185</i> + <i>318</i> = ?
3-digit number + 2-digit number	Use place value equipment to make and combine groups to model addition.	Use a place value grid to organise thinking and adding of 1s, then 10s.	Use the vertical column method to represent the addition. Children must understand how this relates to place value at each stage of the calculation.
3-digit number + 2-digit number, exchange required	Use place value equipment to model addition and understand where exchange is required. Use place value counters to represent 154 + 72. Use this to decide if any exchange is required. There are 5 tens and 7 tens. That is 12 tens so I will exchange.	Represent the required exchange on a place value grid using equipment. 275 + 16 = ? H T O H T O Z75 + 16 = 291 275 + 16 = 291 Note: In this example, a mental method may be more efficient. The numbers for the example calculation have been chosen to	Use a column method with exchange. Children must understand how the method relates to place value at each stage of the calculation. $\boxed{\begin{array}{c} H \\ \hline \hline$





		allow children to visualise the concept and see how the method relates to place value. Children should be encouraged at every stage to select methods that are accurate and efficient.	
Representing addition problems, and selecting appropriate methods	Encourage children to use their own drawings and choices of place value equipment to represent problems with one or more steps. These representations will help them to select appropriate methods.	Children understand and create bar models to represent addition problems. 275 + 99 = ? 374 275 + 99 = 374 275 + 99 = 374	Use representations to support choices of appropriate methods. $\begin{array}{c c} \hline 275 & qq\\\hline 275 & qq\\\hline 275 & qq\\\hline 1 & will add 100, then subtract 1 to find the solution.\\ \hline 128 + 105 + 83 = ?\\\hline 1 & need to add three numbers.\\ \hline 128 + 105 = 233 \\ \hline 128 & 105 & 83\\\hline \hline 128 & 105 & 83\\\hline \hline 233 & 83\\\hline \end{array}$
Year 3 Subtraction			
Subtracting 100s	Use known facts and unitising to subtract multiples of 100.	Use known facts and unitising to subtract multiples of 100.	Understand the link with counting back in 100s.





	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	4 - 2 = 2 400 - 200 = 200	400 - 200 = 200 Use known facts and unitising as efficient and accurate methods. $I  know that  7 - 4 = 3.  Therefore, I know that  700 - 400 = 300.$
3-digit number − 1s, no exchange	Use number bonds to subtract the 1s. Use number bonds to subtract the 1s. 214 - 3 = ? 4 - 3 = 1 214 - 3 = 211	Use number bonds to subtract the 1s. $\begin{array}{c c} H & T & O \\ \hline  & & & \\  & & & \\ \hline  & & & \\  & & & \\ \hline  & & & \\  & & $	Understand the link with counting back using a number line. Use known number bonds to calculate mentally. 476 - 4 = ? 476 476 476 476 6 - 4 = 2 476 - 4 = 472
3-digit number − 1s, exchange or bridging	Understand why an exchange is necessary by exploring why 1 ten must be exchanged.	Represent the required exchange on a place value grid.	Calculate mentally by using known bonds. 151 – 7 = ?





required	Use place value equipment.	151 - 7 = ? $H T O$ $H T O$ $H T O$ $H T O$ $R R R R R$	151 - 1 - 6 = 144
3-digit number − 10s, no exchange	Subtract the 10s using known bonds. 381 - 10 = ? 8 tens with 1 removed is 7 tens. 381 - 10 = 371	Subtract the 10s using known bonds. $\begin{array}{c c} H & T & O \\ \hline                                  $	Use known bonds to subtract the 10s mentally. 372 - 50 = ? 70 - 50 = 20 So, 372 - 50 = 322
3-digit number − 10s, exchange or bridging required	Use equipment to understand the exchange of 1 hundred for 10 tens.	Represent the exchange on a place value grid using equipment. 210 - 20 = ?	Understand the link with counting back on a number line. Use flexible partitioning to support the calculation. 235 - 60 = ?

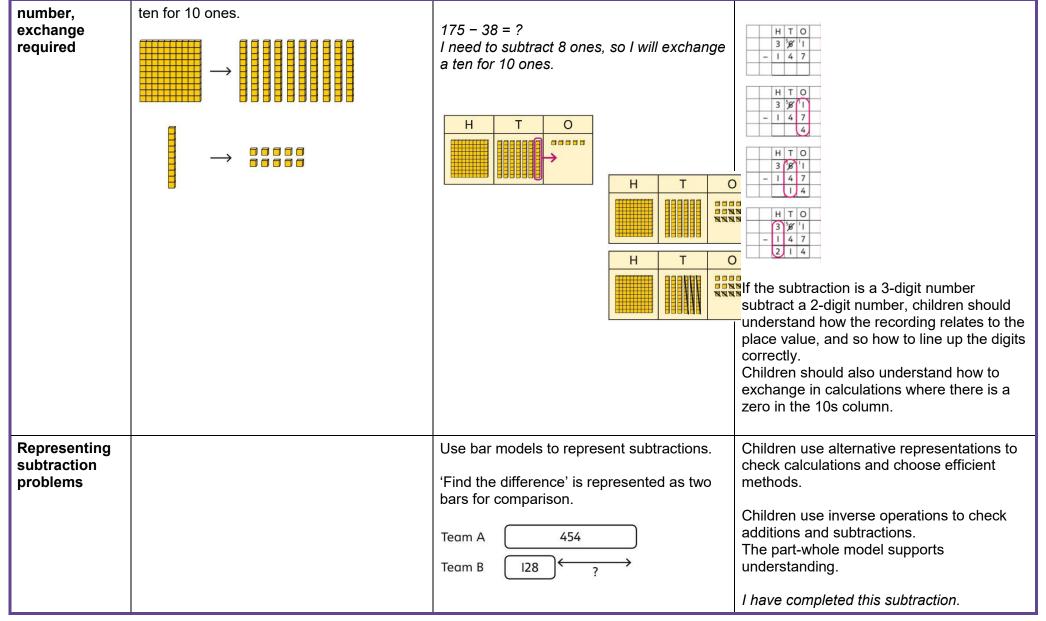




		H       T       O         Ineed to exchange 1 hundred for 10 tens, to help subtract 2 tens.         H       T       O         Image: H       T       O         Ima	235 $235 = 100 + 130 + 5$ $235 - 60 = 100 + 70 + 5$ $= 175$
3-digit number − up to 3-digit number	Use place value equipment to explore the effect of splitting a whole into two parts, and understand the link with taking away.	Represent the calculation on a place value grid.	Use column subtraction to calculate accurately and efficiently.
3-digit number – up to 3-digit	Use base 10 equipment to enact the exchange of 1 hundred for 10 tens, and 1	Model the required exchange on a place value grid.	Use column subtraction to work accurately and efficiently.











		Bar models can also be used to show that a part must be taken away from the whole.	$525 - 270 = 255$ <i>I will check using addition.</i> $\begin{array}{r rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
Year 3 Multiplication			
Understanding equal grouping and repeated addition	Children continue to build understanding of equal groups and the relationship with repeated addition. They recognise both examples and non- examples using objects.	Children recognise that arrays demonstrate commutativity.	Children understand the link between repeated addition and multiplication. 43 + 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 +





	I can see 3 groups of 8. I can see 8 groups of 3.		
Using commutativity to support understanding of the times- tables	Understand how to use times-tables facts flexibly.	Understand how times-table facts relate to commutativity.	Understand how times-table facts relate to commutativity. <i>I need to work out 4 groups of 7.</i> <i>I know that 7 × 4 = 28</i> <i>so, I know that</i>
	There are 6 groups of 4 pens. There are 4 groups of 6 bread rolls.	$6 \times 4 = 24$ $4 \times 6 = 24$	4 groups of 7 = 28 and 7 groups of 4 = 28.
	I can use $6 \times 4 = 24$ to work out both totals.		
Understanding and using ×3,	Children learn the times-tables as 'groups of' but apply their knowledge of	Children understand how the ×2, ×4 and ×8 tables are related through repeated	Children understand the relationship between related multiplication and division

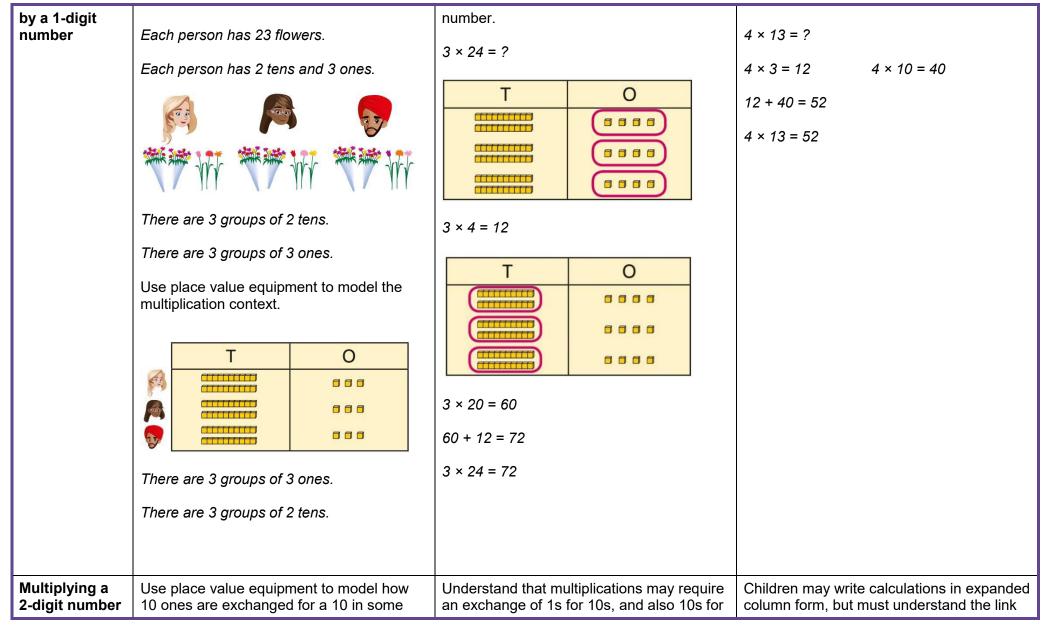




×2, ×4 and ×8 tables.	commutativity.	doubling.	facts in known times-tables.
	Image: Second system       Image: Second system         Image: Second	3 × 2 = 6 3 × 4 = 12 3 × 8 = 24	$ \begin{array}{c} 10 \\ 5 \\ 2 \times 5 = 10 \\ 5 \times 2 = 10 \\ 10 \div 5 = 2 \\ 10 \div 2 = 5 \end{array} $
Using known facts to multiply 10s, for example 3 × 40	Explore the relationship between known times-tables and multiples of 10 using place value equipment. <i>Make 4 groups of 3 ones.</i>	Understand how unitising 10s supports multiplying by multiples of 10.	Understand how to use known times-tables to multiply multiples of 10. $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
	Make 4 groups of 3 tens.	$\begin{array}{c ccccc} 10 & 10 & 10 & 10 \\ \hline 10 & 10 & 10 & 10 \\ \hline 10 & 10 & 10 & 10 \\ \hline 4 \ groups \ of \ 2 \ ones \ is \ 8 \ ones. \\ 4 \ groups \ of \ 2 \ tens \ is \ 8 \ tens. \end{array}$	$\begin{array}{c} +20 +20 +20 +20 \\ \hline 0 & 10 & 20 & 30 & 40 & 50 & 60 & 70 & 80 \end{array}$ $4 \times 2 = 8 \\ 4 \times 20 = 80 \end{array}$
		$4 \times 2 = 8$ $4 \times 20 = 80$	
Multiplying a 2-digit number	Understand how to link partitioning a 2-digit number with multiplying.	Use place value to support how partitioning is linked with multiplying by a 2-digit	Use addition to complete multiplications of 2-digit numbers by a 1-digit number.

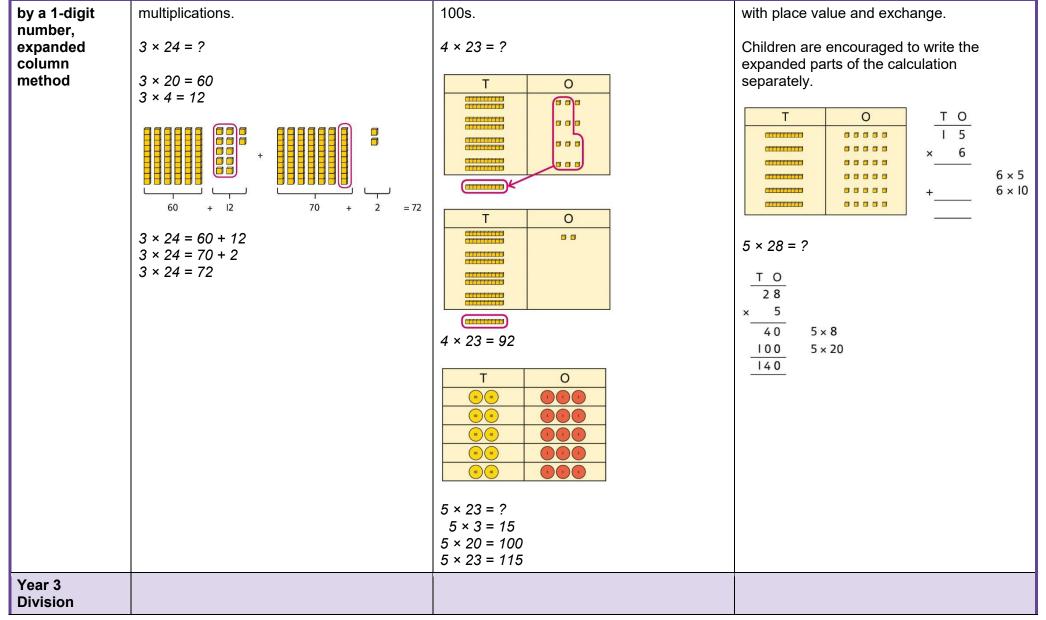
















Using times- tables knowledge to divide	Use knowledge of known times-tables to calculate divisions. 24 divided into groups of 8. There are 3 groups of 8.	Use knowledge of known times-tables to calculate divisions. Use knowledge of known times-tables to calculate divisions. $48 \div 4 = 12$ 48  divided into groups of 4. There are 12 groups. $4 \times 12 = 48$ $48 \div 4 = 12$	Use knowledge of known times-tables to calculate divisions. <i>I need to work out 30 shared between 5.</i> <i>I know that</i> $6 \times 5 = 30$ so <i>I know that</i> $30 \div 5 = 6$ . A bar model may represent the relationship between sharing and grouping. 24 4 4 4 4 4 4 4 4 4
Understanding remainders	Use equipment to understand that a remainder occurs when a set of objects	Use images to explain remainders.	Understand that the remainder is what cannot be shared equally from a set.





Using known facts to divide multiples of 10	cannot be divided equally any further.	22 ÷ 5 = 4 remainder 2 Divide multiples of 10 by unitising. 12 tens shared into 3 equal groups. 4 tens in each group.	$22 \div 5 = ?$ $3 \times 5 = 15$ $4 \times 5 = 20$ $5 \times 5 = 25 \dots \text{ this is larger than } 22$ So, $22 \div 5 = 4 \text{ remainder } 2$ Divide multiples of 10 by a single digit using known times-tables. $180 \div 3 = ?$ $180 \text{ is } 18 \text{ tens.}$ $18 \text{ divided by } 3 \text{ is } 6.$ $18 \text{ tens divided by } 3 \text{ is } 6 \text{ tens.}$ $18 \div 3 = 6$ $180 \div 3 = 60$
2-digit number divided by 1-digit number, no remainders	Children explore dividing 2-digit numbers by using place value equipment.	Children explore which partitions support particular divisions.	Children partition a number into 10s and 1s to divide where appropriate. 60 + 2 = 30 $8 + 2 = 4$ $68 + 2 = 34$ Children partition flexibly to divide where





	Then divide the 1s.	3. 42 30 12 30 12	appropriate. $42 \div 3 = ?$ 42 = 40 + 2 <i>I need to partition 42 differently to divide</i> <i>by 3.</i> 42 = 30 + 12 $30 \div 3 = 10$ $12 \div 3 = 4$ 10 + 4 = 14 $42 \div 3 = 14$
2-digit number divided by 1-digit number, with remainders	Use place value equipment to understand the concept of remainder. <i>Make 29 from place value equipment.</i> <i>Share it into 2 equal groups.</i> There are two groups of 14 and 1 remainder.	Use place value equipment to understand the concept of remainder in division. 29 ÷ 2 = ? 29 ÷ 2 = 14 remainder 1	<ul> <li>Partition to divide, understanding the remainder in context.</li> <li>67 children try to make 5 equal lines.</li> <li>67 = 50 + 17 50 ÷ 5 = 10</li> <li>17 ÷ 5 = 3 remainder 2 67 ÷ 5 = 13 remainder 2</li> <li>There are 13 children in each line and 2 children left out.</li> </ul>





		Year 4	
	Concrete	Pictorial	Abstract
Year 4 Addition			
Understanding numbers to 10,000	Use place value equipment to understand the place value of 4-digit numbers.	Represent numbers using place value counters once children understand the relationship between 1,000s and 100s. 1000 000 00 00 00 00 00 00 00 00 00 00 0	Understand partitioning of 4-digit numbers, including numbers with digits of 0. 5,000 + 60 + 8 = 5,068 Understand and read 4-digit numbers on a number line.
Choosing mental methods where appropriate	Use unitising and known facts to support mental calculations. <i>Make 1,405 from place value equipment.</i> <i>Add 2,000.</i> <i>Now add the 1,000s.</i> <i>1 thousand + 2 thousands = 3 thousands</i> <i>1,405 + 2,000 = 3,405</i>	Use unitising and known facts to support mental calculations. Th H T O O O O O O O O O O O O O O	Use unitising and known facts to support mental calculations. 4,256 + 300 = ? 2 + 3 = 5 200 + 300 = 500 4,256 + 300 = 4,556





Column addition	Use place value equipment on a place value grid to organise thinking. Ensure that children understand how the	Use place value equipment to model required exchanges.	Use a column method to add, including exchanges.
	columns relate to place value and what to do if the numbers are not all 4-digit numbers.		Th     H     T     O       I     5     5     4       +     4     2     3     7
	Use equipment.to show 1,905 + 775.		Th     H     T     O       I     5     5     4       +     4     2     3     7       9     1     1     1
	Why have only three columns been used for the second row? Why is the Thousands box empty?		Th         H         T         O           I         5         5         4           +         4         2         3         7
	Which columns will total 10 or more?		7 9 1 1 Th H T O 1 5 5 4
		Include examples that exchange in more than one column.	Include examples that exchange in more than one column.
Representing additions and		Bar models may be used to represent additions in problem contexts, and to justify	Use rounding and estimating on a number line to check the reasonableness of an





checking strategies		mental methods where appropriate.						addition.
		I,225           799         574				5	574	0 1,000 2,000 3,000 4,000 5,000 6,000 7,000 8,000 9,000 10,000 912 + 6,149 = ?
			Th	H 7	T	0 9		<i>I used rounding to work out that the answer should be approximately 1,000 + 6,000 = 7,000.</i>
		+		5	7	4		
		-	1	3	7	3		
		<i>I chose to work out 574 + 800, then subtract 1.</i>						
		This is equivalent to 3,000 + 3,000.						
Year 4 Subtraction								
Choosing mental methods where appropriate	Use place value equipment to justify mental methods.	metho	ods v <sub>h</sub>	vhere	е ар н	prop	o support mental riate.	Use knowledge of place value and unitising to subtract mentally where appropriate. 3,501 – 2,000 3 thousands – 2 thousands = 1 thousand





	What number will be left if we take away 300?	7,646 - 40 = 7,606	3,501 - 2,000 = 1,501
Column subtraction	Understand why exchange of a 1,000 for 100s, a 100 for 10s, or a 10 for 1s may be necessary.	Represent place value equipment on a place value grid to subtract, including exchanges where needed.	Use column subtraction, with understanding of the place value of any exchange required.





			Th       H       T       O         I       2       5       0         -       3       2       0         Th       H       T       O         I       2       5       0         -       3       2       0         -       3       2       0         -       3       2       0         -       3       2       0         -       3       2       0         -       3       2       0         -       3       2       0         -       3       2       0         -       3       2       0         -       3       2       0         -       3       2       0         -       3       2       0         -       3       2       0         -       3       2       0         -       3       2       0         -       3       2       0
Column subtraction with exchange across more than one column	Understand why two exchanges may be necessary. 2,502 - 243 = ?	Make exchanges across more than one column where there is a zero as a place holder. 2,502 - 243 = ?	Make exchanges across more than one column where there is a zero as a place holder. 2,502 - 243 = ?





	Th H T O	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Representing subtractions and checking strategies	Use bar models to represent subtractions where a part needs to be calculated. Total 5,762 ? ? ? Yes votes <i>I can work out the total number of Yes votes</i> <i>using 5,762 – 2,899.</i> Bar models can also represent 'find the difference' as a subtraction problem.	Use inverse operations to check subtractions. <i>I calculated 1,225 – 799 = 574.</i> <i>I will check by adding the parts.</i>





		Danny 899 ← ? Luis I,005	Th       H       T       O         7       9       9         +       5       7       4         1       3       7       3         i       i       i       i         The parts do not add to make 1,225.       I must have made a mistake.
Year 4 Multiplication			
Multiplying by multiples of 10 and 100	Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.	Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100. $3 \times 4 = 12$ $3 \times 40 = 120$ $3 \times 400 = 1,200$	Use known facts and understanding of place value and commutativity to multiply mentally. $4 \times 7 = 28$ $4 \times 70 = 280$ $40 \times 7 = 280$ $4 \times 700 = 2,800$ $400 \times 7 = 2,800$
Understanding times-tables up to 12 × 12	Understand the special cases of multiplying by 1 and 0.	Represent the relationship between the ×9 table and the ×10 table.	Understand how times-tables relate to counting patterns. Understand links between the ×3 table, ×6 table and ×9 table 5 × 6 is double 5 × 3 ×5 table and ×6 table I know that 7 × 5 = 35





	5 × 1 = 5 5 × 0 = 0	$2 \times 11 = 20 + 2$ $3 \times 11 = 30 + 3$ $4 \times 11 = 40 + 4$	so I know that $7 \times 6 = 35 + 7$ . ×5 table and ×7 table $3 \times 7 = 3 \times 5 + 3 \times 2$ $3 \times 5$ $3 \times 2$ $3 \times 5$ $3 \times 2$ $3 \times 7$ $3 \times 7$ $3 \times 9$ table and ×10 table $6 \times 9 = 60 - 6$
Understanding and using partitioning in multiplication	Make multiplications by partitioning. $4 \times 12$ is 4 groups of 10 and 4 groups of 2. $4 \times 12 = 40 + 8$	Understand how multiplication and partitioning are related through addition. Understand how multiplication and Understand how multiplication and Under	Use partitioning to multiply 2-digit numbers by a single digit. $18 \times 6 = ?$ $18 \times 6 = ?$ $18 \times 6 = 10 \times 6 + 8 \times 6$ $= 60 + 48$ $= 108$
Column multiplication	Use place value equipment to make multiplications.	Use place value equipment alongside a column method for multiplication of up to	Use the formal column method for up to 3-digit numbers multiplied by a single digit.





for 2- and 3-digit numbers multiplied by a single digit	Make 4 × 136 using equipment.	3-digit numbers by a single digit.	$\begin{array}{r} 3     2 \\ \times \underline{3} \\ \underline{3} \\ \underline{4} \\ 3 \\ \underline{3} \\ \underline{4} \\ 3 \\ \underline{6} \\ \underline{3} \\ \underline{6} \\ \underline{7} \\ \underline$
Multiplying more than two numbers	Represent situations by multiplying three numbers together. i = 1 + 1 + 2 + 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3	Understand that commutativity can be used to multiply in different orders. 000000000000000000000000000000000000	Use knowledge of factors to simplify some multiplications. $24 \times 5 = 12 \times 2 \times 5$ $12 \times 2 \times 5 =$ $12 \times 10 = 120$ So, $24 \times 5 = 120$





Year 4 Division			
Understanding the relationship between multiplication and division, including times-tables	Use objects to explore families of multiplication and division facts.	Represent divisions using an array.	Understand families of related multiplication and division facts. <i>I know that 5</i> × 7 = 35
			so I know all these facts:
	4 × 6 = 24 24 is 6 groups of 4. 24 is 4 groups of 6. 24 divided by 6 is 4. 24 divided by 4 is 6.	28 ÷ 7 = 4	$5 \times 7 = 35$ $7 \times 5 = 35$ $35 = 5 \times 7$ $35 = 7 \times 5$ $35 \div 5 = 7$ $35 \div 7 = 5$ $7 = 35 \div 5$ $5 = 35 \div 7$
Dividing multiples of 10 and 100 by a single digit	Use place value equipment to understand how to use unitising to divide.	Represent divisions using place value equipment. $q_{\pm 3} =$ $q_{\pm 3} =$ $q_{\pm 3} =$ $q_{0 \pm 3} =$	Use known facts to divide 10s and 100s by a single digit. $15 \div 3 = 5$ $150 \div 3 = 50$ $1500 \div 3 = 500$
	8 hundreds divided into 2 equal groups	9 tens divided by 3 is 3 tens. 9 hundreds divided by 3 is 3 hundreds.	





	4 hundreds in each group		
Dividing 2-digit and 3-digit numbers by a single digit by partitioning into 100s, 10s and 1s	Partition into 10s and 1s to divide where appropriate.	Partition into 100s, 10s and 1s using Base 10 equipment to divide where appropriate.	Partition into 100s, 10s and 1s using a part- whole model to divide where appropriate.
	39 ÷ 3 = ?	39 ÷ 3 = ?	142 ÷ 2 = ?
	$3 \times 10 = 30$ $3 \times 3 = 9$	3 groups of I ten 3 groups of 3 ones	146 $100 + 2 = 40 + 2 = 6 + 2 = 1$
	39 = 30 + 9	39 = 30 + 9	$100 \div 2 = 50$
	30 ÷ 3 = 10	30 ÷ 3 = 10	$40 \div 2 = 20$ $6 \div 2 = 3$
	$9 \div 3 = 3$ $39 \div 3 = 13$	$9 \div 3 = 3$ $39 \div 3 = 13$	50 + 20 + 3 = 73 142 ÷ 2 = 73
Dividing 2-digit and 3-digit	Use place value equipment to explore why different partitions are needed.	Represent how to partition flexibly where needed.	Make decisions about appropriate partitioning based on the division required.
numbers by a single digit, using flexible	42 ÷ 3 = ?	84 ÷ 7 = ?	
partitioning	I will split it into 30 and 12, so that I can divide by 3 more easily.	<i>I will partition into 70 and 14 because I am dividing by 7.</i>	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
		$ \begin{array}{c} 84 \\ 70 \div 7 = 10 \\ 84 \div 7 = 2 \end{array} $	Understand that different partitions can be used to complete the same division.





			$ \begin{array}{c}             132 \\             60 + 3 = 20 & 60 + 3 = 20 & 12 + 3 = 4 \\             132 + 3 = 44 \\             132 + 3 = 44 \\             132 \\             120 + 3 = 40 \\             120 + 3 = 40 \\             12 + 3 = 4 \\             132 \\             120 + 3 = 40 \\             120 $
Divide by sharing	Share using place value equipment	Share by exchanging	Share using known facts and partitioning where appropriate $142 \div 2 = ?$ $142 \div 2 = ?$ $142 \div 2 = ?$ $100 \div 2 = 40 \div 2 = 6 \div 2 = 1$ $100 \div 2 = 50$ $40 \div 2 = 20$ $6 \div 2 = 3$ 50 + 20 + 3 = 73 $142 \div 2 = 73$
Understanding remainders	Use place value equipment to find remainders. 85 shared into 4 equal groups There are 24, and 1 that cannot be shared.	Represent the remainder as the part that cannot be shared equally.	Understand how partitioning can reveal remainders of divisions.





	72 ÷ 5 = 14 remainder 2	80 ÷ 4 = 20 12 ÷ 4 = 3 95 ÷ 4 = 23 remainder 3
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